

# PHYS/MATH 611 -- Mathematical Physics I -- Fall 2017

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|-------------------|---|
| Instructor:       | Chung-Sang Ng   |
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| Class meets:      | MWF 10:30 AM - 11:30 AM, Reichardt 204  |
| Office hours:     | MWF 9:25 AM - 10:25 AM or by appointment  |
| Credits:          | 3 credits: 3 hours/week of lecture.   |
| Textbook:         | "Mathematical Methods for Physicists", 7th ed., by Arfken, Weber, and Harris  |
| Prerequisites:    | Graduate standing   |
| Course Home Page: | <a href="http://www.gi.alaska.edu/~chungsangng/phys611/phys611.html">http://www.gi.alaska.edu/~chungsangng/phys611/phys611.html</a> |

## I. Course Description

The UAF Catalog listing for PHYS 611: "Mathematical tools and theory for classical and modern physics. Core topics: linear algebra including eigenvalues, eigenvectors and inner products in finite dimensional spaces. Infinite series. Hilbert spaces and generalized functions. Complex analysis, including Laurent series and contour methods. Applications to problems arising in physics. Selected additional topics, which may include operator and spectral theory, groups, tensor fields and hypercomplex numbers."

In terms of the content of the textbook (which you must have and bring to classes), we will try to cover most topics from Chapter 4 to 12 during the fall semester, with Chapter 1 to 3 treated as background that students should review themselves. We will not cover everything in these chapters, due to the fact that we only have limited amount of time, not because other topics are not important. At the end of this syllabus is a tentative schedule which lists topics we plan to cover in more details. This is subject to change. So you should check frequently the online version of this page: <http://www.gi.alaska.edu/~chungsangng/phys611/phys611.html>

## II. Course Goals

The main goal of this course is to introduce you to some fundamental advanced mathematical methods for physics at the beginning graduate level to help students learning better in other graduate physics courses and doing research in their graduate studies. Emphasis will be on application aspects of the subject rather than proofs of theorems.

## III. Student Learning Outcomes

- Know how to apply some advanced mathematical methods to solve physics problems.
- Be able to solve most PhD Mathematical Physics comprehensive exam questions in recent

years.

- Can apply rigorous mathematical and logical manipulations in the study and research of physics.

#### **IV. Textbook**

You must have a copy of the textbook: "Mathematical Methods for Physicists", 7th ed., by Arfken, Weber, and Harris. It is very important that you read the Section(s) covered within each lecture and try to follow derivations before you come to that lecture. Please refer to the schedule below (subject to change) for such reading assignments. You should bring your textbook to the lectures.

You will find it extremely useful to have some mathematical references, handbooks, or tables, e.g., table of integrals. There are many options available from the Internet, but you should be cautious about the accuracy of information obtained there. One recommendation is [Abramowitz and Stegun: Handbook of Mathematical Functions](#), which can be downloaded freely. Another one is [Gradshteyn and Ryzhik](#). A handy collection of useful formula is the [NRL Plasma Formulary](#), which you can order a free copy or download it online.

#### **V. Instructional method and reading assignments**

The course is for 3 credits, and so 3 hours per week are devoted to "lectures" in the classroom. However, since this is a graduate level course and that the topics and mathematics are quite advanced, there is not enough time to explain everything in details by lecturing. Students must help themselves by reading and studying before each class. You are expected to ask questions and contribute to discussion in class. I will not have time to go through all the text and derivations, but will try to answer questions that you found difficult. Any materials that we don't have time to go through in that class have to be left for self-study by students themselves. If you still have difficulties, you need to come to my office hours (or set up another time) and ask for additional help.

#### **VI. Participation grade**

To encourage you to finish reading assignments before classes and to practice what we are learning, 10% of the final grade is for participation. During some lectures, we will do some practice questions. You can write down your answers and derivation on pieces of paper and hand in at the end of the lecture. It is graded heavily on effort and participation instead of correctness of your answers. An absence will result in no participation grade unless it is excused based on documented reasons (e.g. research trip, sickness, or emergency). However, since I will not count the five lowest grades, those can be used for unexcused absences.

#### **VII. Homework**

Doing homework is the most important factor in doing well in this class. There will be approximately one homework set assigned per week, usually on Fridays, and is usually due in the following Friday before class. However, you should work on your homework as early as possible before a deadline so that you can have time to ask for help during classes or in my office hours if you encounter difficulties in solving these problems. Late homework will not be accepted.

To emphasize the importance of doing homework, homework grade will count towards 30% of the

total grade of the course, excluding the assignment with the lowest grade. I will grade the homework based on your effort, the method used, as well as the correctness of answers. Therefore, you should submit your partially finished work. This will help you getting partial credit, and let me identify your difficulties. Also, your work should be clean and clear enough for me to understand.

While it is good for you to have discussion with classmates or search the Internet for additional information, your submitted homework should be of your own, but not a direct copy from another source. If you finish a question with the help of another person, a solution book, or a solution you found in the Internet or passed on to you from another student, you need to cite that at the end of your answer for that question. There is no deduction of points for using help that you cited if it is not a direct copy. However there can be deduction up to the maximum points of that homework set if you used help but failed to cite. Also, you should use help only to enable you to do a problem yourselves. Keep in mind that you will be required to do similar questions on your own during exams (closed books in the exams, and also in the PhD comprehensive exam). In addition, it is against the UAF Honor Code to misrepresent work which is not your own. Plagiarism on homework or on an exam will result in a failing grade.

Solutions to the homework problems will be available to you after the due date. Therefore, late homework will not be accepted. The homework assignments will be posted on Blackboard.

### VIII. Examinations

There will be an one-hour in-class midterm exam on Friday, October 20, and a two-hour final exam on Wednesday December 13 from 10:15 AM to 12:15 PM. They are closed book exams with questions at a level similar to those in past PhD comprehensive exams. Calculators, computers, and communication devices are also not allowed. However, special or unusual formula or integrals essential to a particular question will be written down for that question. Midterm exam counts towards 20% of the total grade. The final exam counts towards 40 % of the total grade. ***You must not miss the midterm exam and the Final Exam (except for documented illness or family emergency ).***

Tips for getting more points in an exam: Exam questions will be graded based on the method used, as well as the answer. Therefore, you should write down explicitly and clearly step by step how you come up with your answers. Even if you don't know how to answer a question (or parts of a question), write down everything you can think of that might help formulate an approach to answer it. If you don't know how to answer the first part of a question, you should move on to answer other parts by assuming an answer to the first part. This will help you getting partial credit.

### IX. Grading

The final grade will be composed of:

|               |      |   |
|---------------|------|---|
| Participation | 10 % | Lowest grades of 5 days are dropped       |
| Midterm exam  | 20 % | Mandatory                                 |
| Final exam:   | 40 % | Mandatory                                 |
| Homework      | 30%  | Homework set with lowest grade is dropped |

|        |       |  |
|--------|-------|--|
| Total: | 100 % |  |
|--------|-------|--|

Midterm and Final exams are mandatory, while Participation and Homework are optional in the sense that grades for each of them will be counted only if it can increase your total grade. If either one or both of them would decrease your total grade, it will be replaced by the average grade of both exams. The course will be graded approximately according to the following scale:

|              |    |
|--------------|----|
| > 90 %       | A  |
| 83 % -- 90 % | A- |
| 76 % -- 83 % | B+ |
| 70 % -- 76 % | B  |
| 63 % -- 70 % | B- |
| 56 % -- 63 % | C+ |
| 50 % -- 56 % | C  |
| 43 % -- 50 % | C- |
| 36 % -- 43 % | D+ |
| 30 % -- 36 % | D  |
| 23 % -- 30 % | D- |
| < 23 %       | F  |

Note that the passing grade for graduate students is B. Therefore, in order to pass this course, you should get most of the points in homework/participation, and to get enough points in exams.

## X. Getting Help

My office hours are 9:25 AM - 10:25 AM on Mondays, Wednesdays, and Fridays. I will be at Reichardt 108 during these office hours. Canceled office hours will be announced in class or by email. If you need to see me beside these office hours, please set up a time by appointment to come to my office at Elvey 706E. These are hours set aside especially to help you - do not feel like you are imposing or cheating by coming in. If you have problems that need immediate attention, please send me an e-mail or give me a call at my office phone number.

I have set up a home page for the course: <http://www.gi.alaska.edu/~chungsangng/phys611/phys611.html> . I may put additional materials that may be helpful to you later. So, please come back often, especially to check any changes in the schedule. The UAF Blackboard site for this course will be made available to students, but will not be used to provide communication about this course. I might post grades there but those might not be updated very frequently.

## XI. Disabilities Services

The Physics Department will work with the Office of Disabilities Services (<http://www.uaf.edu/disability/>) to provide reasonable accommodation to students with disabilities.

## XII. Tentative Schedule

Below is a tentative schedule (subject to change):

| Date  | Day | Text<br>(Reading<br>Assignment) | Main Topics   | Homework<br>due |
|-------|-----|---------------------------------|---|-----------------|
| 8/28  | M   | Ch1-3                           | Review of Mathematical Preliminaries                              |                 |
| 9/1   | W   | 11.1-2                          | Complex Variables and Functions/Cauchy-Riemann<br>Conditions      |                 |
| 9/3   | F   | 11.3                            | Cauchy's Integral Theorem   |                 |
| 9/6   | W   | 11.4                            | Cauchy's Integral Formula   |                 |
| 9/8   | F   | 11.5                            | Laurent Expansion   | HW #1           |
| 9/11  | M   | 11.6                            | Singularities   |                 |
| 9/13  | W   | 11.7                            | Calculus of Residues  |                 |
| 9/15  | F   | 11.8                            | Evaluation of Definite Integrals                                  | HW #2           |
| 9/18  | M   | 11.9-10                         | Evaluation of Sums/Conformal Mapping                              |                 |
| 9/20  | W   | 4.1-2                           | Tensor Analysis/Pseudotensors, Dual Tensors                       |                 |
| 9/22  | F   | 4.3                             | Tensors in General Coordinates                                    | HW #3           |
| 9/25  | M   | 4.4                             | Jacobians   |                 |
| 9/27  | W   | 5.1                             | Vectors in Function Spaces  |                 |
| 9/29  | F   | 5.2                             | Gram-Schmidt Orthogonalization                                    | HW #4           |
| 10/2  | M   | 5.3                             | Operators   |                 |
| 10/4  | W   | 5.4-5                           | Self-Adjoint Operators/Unitary Operators                          |                 |
| 10/6  | F   | 5.6-8                           | Transformations of Operators/Invariants                           | HW #5           |
| 10/9  | M   | 6.1-2                           | Eigenvalue Equations/Matrix Eigenvalue Problems                   |                 |
| 10/11 | W   | 6.3-4                           | Hermitian Eigenvalue Problems/Hermitian Matrix<br>Diagonalization |                 |
| 10/13 | F   | 6.5                             | Normal Matrices   | HW #6           |
| 10/16 | M   | 7.1-2                           | Ordinary Differential Equations/First-Order<br>Equations          |                 |
| 10/18 | W   | 7.3-4                           | ODEs with Constant Coefficients/Second-Order<br>Linear ODEs       |                 |
| 10/20 | F   |                                 | Mid-term exam   | HW #7           |

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|-------|---|--------|---|--------|
| 10/23 | M | 7.5    | Series Solutions - Frobenius' Method  |        |
| 10/25 | W | 7.6    | Other Solutions   |        |
| 10/27 | F | 7.7-8  | Inhomogeneous Linear ODEs/Nonlinear Differential Equations  | HW #8  |
| 10/30 | M | 8.1-2  | Sturm-Liouville Theory/Hermitian Operators  |        |
| 11/1  | W | 8.3-5  | ODE Eigenvalue Problems/Variation Method  |        |
| 11/3  | F | 9.1-2  | Partial Differential Equations/First-Order Equations  | HW #9  |
| 11/6  | M | 9.3    | Second-Order Equations  |        |
| 11/8  | W | 9.4    | Separation of Variables   |        |
| 11/10 | F | 9.5-6  | Laplace and Poisson Equations/Wave Equation   | HW #10 |
| 11/13 | M | 9.7-8  | Heat-Flow, or Diffusion PDE   |        |
| 11/15 | W | 10.1   | Green's Functions/One-Dimensional Problems  |        |
| 11/17 | F | 10.2   | Problems in Two and Three Dimensions  | HW #11 |
| 11/20 | M | 12.1   | Orthogonal Polynomials  |        |
| 11/22 | W | 12.2   | Bernoulli Numbers   |        |
| 11/27 | M | 12.3   | Euler-Maclaurin Integration Formula   |        |
| 11/29 | W | 12.4-5 | Dirichlet Series/Infinite Products  |        |
| 12/1  | F | 12.6   | Asymptotic Series   | HW #12 |
| 12/4  | M | 12.7   | Method of Steepest Descents   |        |
| 12/6  | W | 12.8   | Dispersion Relations  |        |
| 12/8  | F |        | Review  |        |
| 12/13 | W |        | Final (10:15 AM to 12:15 PM)  |        |
| 12/18 | M |        | This is absolutely the last day for submitting your report to me,<br>as well as discussing with me about your grades. |        |
| 12/20 | W |        | Final grades will be submitted by noon.<br>They will also be posted on Blackboard.                                    |        |